

Curve Sketching: Analyzing a Graph

Ex)  $f(x) = \frac{2(x^2-9)}{x^2-4} = 0$   $f(0) = 9/2$  HA:  $\frac{2x^2}{x^2} = 2$

$f'(x) = \frac{20x}{(x^2-4)^2}$

$f''(x) = \frac{-20(3x^2+4)}{(x^2-4)^3}$

$0 = \frac{20x}{(x^2-4)^2}$

$0 = \frac{-20(3x^2+4)}{(x^2-4)^3}$

\* x-intercepts: 3, -3

\* horiz asymp: 2

\* y-intercept: 9/2

\* crit #'s = -2, 2, 0

|          | $(-\infty, -2)$ | $(-2, 0)$ | $(0, 2)$ | $(2, \infty)$ | characteristics          |
|----------|-----------------|-----------|----------|---------------|--------------------------|
| $f(x)$   | undef           | 9/2       | undef    | undef         | decreasing, concave down |
| $f'(x)$  | -               | 0         | +        | -             | vert asymp               |
| $f''(x)$ | -               | +         | +        | -             | decreasing, concave up   |
|          |                 |           |          |               | relative minimum         |
|          |                 |           |          |               | increasing, concave up   |
|          |                 |           |          |               | vert asymp               |
|          |                 |           |          |               | increasing, concave down |

